

Some solutions for 3.3 Practice.

1. a) $\frac{1}{4}(x-3) = -2$ multiply both side by 4

$$\begin{array}{r} x-3 = -8 \\ +3 \quad +3 \end{array}$$

add 3 to both sides

$$\boxed{x = -5}$$

b) $6 = -\frac{3}{5}(a-7)$ multiply both sides by 5

$$30 = -3(a-7)$$

divide both sides by -3

$$\begin{array}{r} -10 = a-7 \\ +7 \quad +7 \end{array}$$

add 7 to both sides

$$-3 = a$$

$$\boxed{a = -3}$$

c) $\frac{m+7}{5} = 3$ multiply both sides by 5

$$\begin{array}{r} m+7 = 15 \\ -7 \quad -7 \end{array}$$

$$\boxed{m = 8}$$

subtract 7 from both sides

2. a) $9 = \frac{3(k+4)}{2}$ multiply both sides by 2.

$$18 = 3(k+4) \quad \div 3$$

$$\begin{array}{r} 6 = k+4 \\ -4 \quad -4 \end{array}$$

$$\boxed{2 = k}$$

$$2b) \quad \frac{3k+5}{2} = 10 \quad \times \text{ by } 2.$$

$$3k+5 = 20 \quad \text{sub. } 5$$
$$\quad \quad -5 \quad -5$$

$$3k = 15 \quad \div 3$$

$$\boxed{k = 5}$$

$$c) \quad 1 = \frac{2p-3}{5} \quad \times \text{ by } 5$$

$$5 = 2p-3 \quad + 3$$
$$\quad \quad +3 \quad +3$$

$$8 = 2p \quad \div 2$$

$$\boxed{4 = p}$$

~~2)~~

$$3a) \quad \frac{y-5}{3} = -4 \quad \times 3$$

$$y-5 = -12. \quad +5$$
$$\quad \quad +5 \quad +5$$

$$\boxed{y = -7}$$

$$b) \quad \frac{1}{3}(p+2) = -5 \quad \times 3$$

$$p+2 = -15 \quad -2$$
$$\quad \quad -2 \quad -2$$

$$\boxed{p = -17}$$

$$c) \quad 3 = \frac{4}{5}(h+2) \quad \times 5$$

$$15 = 4(h+2) \quad \div 4$$

$$\frac{15}{4} = h+2 \quad -2$$

$$3.75 = h+2$$
$$\quad \quad -2$$

$$\boxed{1.75 = h}$$

$$\text{or } \boxed{\frac{7}{4}}$$

$$\#4. a) \quad 5 = \frac{4(n+3)}{2} \quad \times 2.$$

$$10 = 4(n+3) \quad \div 4$$

$$\frac{10}{4} = n+3$$

$$2.5 = n+3 \quad -3$$

$$\boxed{-0.5 = n}$$

$$b) \quad 6 = \frac{7-c}{2} \quad \times 2$$

$$12 = 7 - c \quad -7$$

$$5 = -c \quad \div -1$$

$$\boxed{-5 = c}$$

$$c) \quad \frac{3+w}{-2} = 4 \quad \times (-2.)$$

$$3+w = -8 \quad -3$$

$$\boxed{w = -11}$$

$$5. a) \quad \frac{h-4}{5} = \frac{h-3}{6} \quad \begin{array}{l} \times \text{LS by } 6 \\ \times \text{RS by } 5 \end{array}$$

$$6(h-4) = 5(h-3)$$

$$6h - 24 = 5h - 15$$

$$\begin{array}{r} 6h - 24 = 5h - 15 \\ +24 \quad \quad +24 \\ \hline 6h = 5h + 9 \\ -5h \quad -5h \\ \hline 1h = 9 \end{array}$$

move 24 to RS

move 5h to LS

$$\boxed{h=9}$$

5b) $\frac{d-2}{4} = \frac{d+1}{3}$ x LS by 3
RS by 4

$$3(d-2) = 4(d+1)$$

$$3d - 6 = 4d + 4$$

add 6

$$\begin{array}{r} 3d - 6 = 4d + 4 \\ +6 \qquad \qquad +6 \\ \hline 3d = 4d + 10 \\ -4d \quad -4d \\ \hline -1d = 10 \end{array}$$

-4d

$$-1d = 10$$

$$\boxed{d = -10}$$

c) $\frac{1}{3}(x+4) = \frac{1}{5}(x+2)$

same as $\frac{x+4}{3} = \frac{x+2}{5}$ x LS by 5
RS by 3

$$5(x+4) = 3(x+2)$$

$$5x + 20 = 3x + 6$$

-20

$$\begin{array}{r} 5x = 3x + 6 \\ -3x \quad -3x \\ \hline 2x = 6 - 20 \\ \hline 2x = -14 \end{array}$$

-3x

$$\frac{2x}{2} = \frac{-14}{2}$$

÷2

$$\boxed{x = -7}$$

$$\#6 a) \frac{1}{4}(p-7) = \frac{1}{6}(p-3) \quad \begin{array}{l} \times \text{LS by } 6 \\ \times \text{RS by } 4 \end{array}$$

$$6(p-7) = 4(p-3)$$

$$6p - 42 = 4p - 12. \quad +42$$

$$\begin{array}{r} 6p = 4p + 30 \\ -4p \quad -4p \\ \hline 2p = 30 \end{array} \quad -4p$$

$$\frac{2p}{2} = \frac{30}{2} \quad \div 2$$

$$\boxed{p=15}$$

$$b) \frac{2(k-5)}{3} = \frac{4(k+2)}{5} \quad \begin{array}{l} \times \text{LS by } 5 \\ \times \text{RS by } 3 \end{array}$$

$$5(2(k-5)) = 3(4(k+2))$$

$$5(2k-10) = 3(4k+8)$$

$$10k - 50 = 12k + 24 \quad +50$$

$$\begin{array}{r} 10k = 12k + 74 \\ -12k \quad -12k \\ \hline -2k = 74 \end{array} \quad -12k$$

$$\frac{-2k}{-2} = \frac{74}{-2} \quad \div -2$$

$$\boxed{k = -37}$$

$$6c) \quad \frac{3(s-4)}{4} = \frac{2(s-3)}{3} \quad \begin{array}{l} \times \text{LS by } 3 \\ \text{RS by } 4. \end{array}$$

$$3(3(s-4)) = 4(2(s-3))$$

$$3(3s-12) = 4(2s-6)$$

$$9s - 36 = 8s - 24 \quad \begin{array}{l} +36 \\ +36 \end{array}$$

$$\begin{array}{r} 9s \\ -8s \end{array} = \begin{array}{r} 8s \\ -8s \end{array} + 12 \quad -8s$$

$$1s = 12$$

$$\boxed{s=12}$$

~~$$7a) \quad \frac{2(3m+2)}{5} = \frac{3(m+5)}{4} \quad \begin{array}{l} \times \text{LS by } 4 \\ \text{RS by } 5 \end{array}$$~~

~~$$4(2(3m+2)) = 5(3(m+5))$$~~

~~$$4(6m+4) = 5(3m+5)$$~~

~~$$24m + 16 = 15m + 25 \quad -16$$~~

~~$$\begin{array}{r} 24m \\ -15m \end{array} = \begin{array}{r} 15m \\ -15 \end{array} + 9 \quad -15m$$~~

$$\begin{aligned} 4(2(3m+2)) &= 5(3(m+5)) \\ 4(6m+4) &= 5(3m+15) \\ 24m+16 &= 15m+75 \\ -15m & \quad -15m \end{aligned}$$

$$9m+16 = 75$$

$$\quad -16 \quad -16$$

$$9m = 59$$

$$\boxed{m = \frac{59}{9}}$$

$$\frac{2}{3}(k+2) = \frac{3}{4}(2k-1)$$

$$4(2(k+2)) = 3(3(2k-1))$$

$$4(2k+4) = 3(6k-3)$$

$$8k+16 = 18k-9$$

$$\quad -16 \quad +16$$

$$8k = 18k - 25$$

$$-18k \quad -18k$$

$$-10k = -25$$

$$k = \frac{-25}{-10} = \boxed{\frac{5}{2}}$$

$$c) \frac{4c+5}{3} = \frac{5(2c+4)}{5}$$

$$5(4c+5) = 3(2c+4)$$

$$20c + 25 = 6c + 12$$

$$\quad \quad -25 \quad \quad \quad -25$$

$$20c = 6c - 13$$

$$\quad -6c \quad \quad -6c$$

$$14c = -13$$

$$c = \frac{-13}{14}$$

$$d) \frac{5-3n}{4} = \frac{2-n}{3}$$

$$3(5-3n) = 4(2-n)$$

$$15 - 9n = 8 - 4n$$

$$\quad -15 \quad \quad \quad -15$$

$$-9n = -7 - 4n$$

$$\quad +4n \quad \quad \quad +4n$$

$$-5n = -7$$

$$n = \frac{-7}{-5} = \frac{7}{5}$$

$$e) \frac{2(3w+4)}{5} = \frac{2(2w-1)}{3}$$

$$3(2(3w+4)) = 5(2(2w-1))$$

$$3(6w+8) = 5(4w-2)$$

$$18w + 24 = 20w - 10$$

$$\quad \quad -24 \quad \quad \quad -24$$

$$18w = 20w - 34$$

$$\quad -20w \quad \quad -20w$$

$$-2w = -34$$

$$\quad \quad -2 \quad \quad \quad -2$$

$$w = 17$$

$$8. \text{ area trapezoid} = \frac{(a+b)h}{2}$$

$$96 = \frac{(6+10)h}{2} \quad (\times 2)$$

$$192 = 16h \quad \div 16$$

$$\boxed{h = 12 \text{ m.}}$$

9. a) $\frac{x+5}{4} = \frac{x-2}{3}$

$4(x+5) = 3(x-2)$ \rightarrow they multiplied wrong way
 \rightarrow should be

$$3(x+5) = 4(x-2)$$

b) $\frac{1}{5}(2y+4) = \frac{1}{2}(y-3)$

$$\frac{10 \times 1(2y+4)}{5} = \frac{10 \times 1}{2}(y-3)$$

\rightarrow they made an error here

$$= 2(2y+4) = 5(y-3)$$

(didn't divide 10 by 5 and 2)

c) $A = \frac{b \times h}{2}$

$$72 = \frac{b \times 8}{2} \quad (\times 2)$$

$$144 = b \times 8 \quad (\div 8)$$

$$\boxed{18 = b}$$

$$\boxed{b = 18 \text{ cm}}$$

$$11. F = \frac{9}{5}C + 32$$

$$\begin{aligned} a) F &= \frac{9(30)}{5} + 32 \\ &= \frac{270}{5} + 32 \\ &= 54 + 32 \\ &= 86^\circ F. \end{aligned}$$

$$b) 77 = \frac{9}{5}C + 32$$

$$\begin{array}{r} -32 \qquad -32 \\ \hline 45 = \frac{9C}{5} \qquad \times 5 \end{array}$$

$$\frac{225}{9} = \frac{9C}{9} \qquad \div 9$$

$$C = 25^\circ C.$$

$$12a) \frac{2a}{3} + \frac{a-4}{5} = \frac{1}{2} \qquad \text{Common value} = 30$$

$$30\left(\frac{2a}{3}\right) + 30\left(\frac{a-4}{5}\right) = \frac{30}{2}$$

$$10(2a) + 6(a-4) = 15$$

$$20a + 6a - 24 = 15$$

$$\begin{array}{r} 26a - 24 = 15 \qquad +24 \\ \hline 26a = 39 \end{array}$$

$$a = \frac{39}{26} \stackrel{\div 13}{=} \frac{3}{2}$$

$$12b) \quad \frac{u+1}{2} + \frac{2u+3}{3} = \frac{u}{4} \quad \text{common}$$

$$12 \frac{(u+1)}{2} + 12 \frac{(2u+3)}{3} = \frac{12u}{4}$$

$$6(u+1) + 4(2u+3) = 3u.$$

$$6u+6 + 8u + 12 = 3u.$$

$$14u + 18 = 3u.$$

$$\begin{array}{r} -14u \\ 18 = 3u - 14u \end{array}$$

$$18 = -11u \quad \text{or} \quad -11u = 18$$

$$\boxed{u = \frac{-18}{11}}$$

$$c) \quad \frac{w+3}{4} = \frac{w}{3} + \frac{2w-1}{5} \quad \text{common} = 60$$

$$60 \frac{(w+3)}{4} = \frac{60w}{3} + 60 \frac{(2w-1)}{5}$$

$$15(w+3) = 20w + 12(2w-1)$$

$$15w + 45 = 20w + 24w - 12$$

$$15w + 45 = 44w - 12$$

$$\begin{array}{r} -45 \\ 15w + 45 = 44w - 12 \\ \hline 15w = 44w - 57 \end{array}$$

$$\begin{array}{r} 15w = 44w - 57 \\ -44w \\ \hline -29w = -57 \end{array}$$

$$-29w = -57$$

$$\boxed{w = \frac{57}{29}}$$